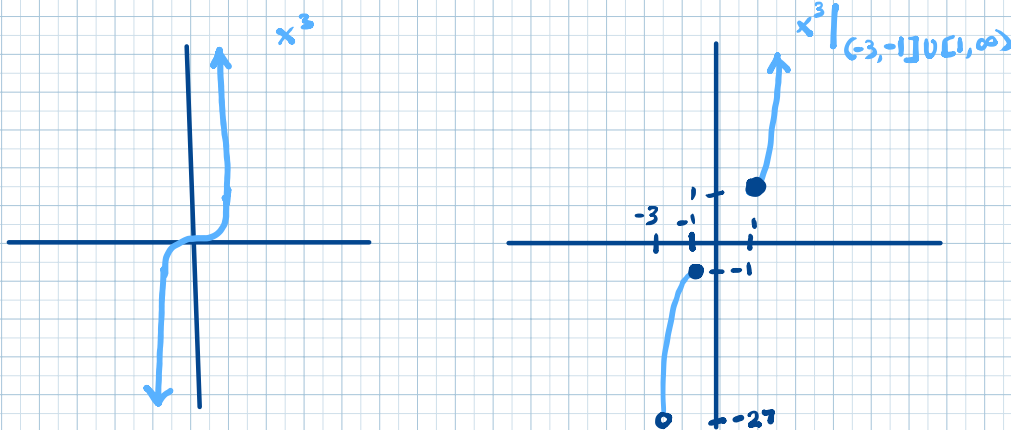
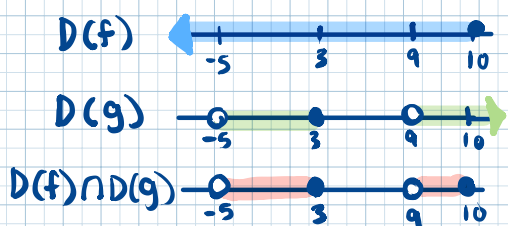


1. Take $f(x) = x^3$. Draw the function on the restriction $(-3, -1] \cup [1, \infty)$.



2. Take f and g to be functions with $\mathcal{D}(f) = (-\infty, 10]$, $\mathcal{D}(g) = (-5, 3] \cup (9, \infty)$, and the zero set of g is $\{3, 11\}$. Determine the domain of $f + g$, fg , and $\frac{f}{g}$.



Domain of
 $f+g$ and fg
is
 $(-5, 3] \cup (9, 10]$

Domain of
 $\frac{f}{g}$ is
 $\mathcal{D}(f) \cap \mathcal{D}(g) \setminus \{3, 11\}$
 $(-5, 3) \cup (9, 10]$

3. Determine how $f - g$ is defined and the domain of $f - g$.

$(f - g)(x) = f(x) - g(x)$, domain of $f - g$ is
definition of $f - g$ $\mathcal{D}(f) \cap \mathcal{D}(g)$

4. Take f and g to be given by

$$f(x) = 2x \quad \text{and} \quad g(x) = \sqrt{x-4}.$$

Determine a formula for $f \circ g$ and $g \circ f$. Also determine the domain of both functions.

$$\bullet (f \circ g)(x) = f(g(x))$$

$$= 2(g(x)) \Rightarrow (f \circ g)(x) = 2\sqrt{x-4}$$

$$= 2\sqrt{x-4}$$

domain of $f \circ g$
need $x-4 \geq 0$

$$[4, \infty) \text{ domain of } f \circ g$$

$$\bullet (g \circ f)(x) = g(f(x))$$

$$= \sqrt{f(x)-4} \Rightarrow (g \circ f)(x) = \sqrt{2x-4}$$

$$= \sqrt{2x-4}$$

domain of $g \circ f$
need $2x-4 \geq 0$

$$[2, \infty) \text{ domain of } g \circ f$$

5. Take

$$a(x) = x, \quad b(x) = x^2, \quad c(x) = x + 3, \quad d(x) = 5x, \quad \text{and} \quad e(x) = \sqrt{x}.$$

Decompose f into sums, products, quotients and or composites of more elementary functions, where

$$f(x) = x^2 \sqrt{x+5x^2} + \frac{x+3}{x}.$$

$$\textcircled{1} \quad x^2 = b \Rightarrow 5x^2 = (dob)(x)$$

$$5x = d$$

$$\textcircled{2} \quad x = a \Rightarrow x+5x^2 = a + dob$$

$$5x^2 = dob$$

$$\textcircled{3} \quad \sqrt{x} = e \Rightarrow \sqrt{x+5x^2} = e \circ (a + dob)$$

$$x+5x^2 = a + dob$$

$$\begin{array}{ccc} \downarrow & \downarrow & \downarrow \\ b \circ e \circ (a + dob) + \frac{c}{a} \end{array}$$