

1. Take  $f$  to be the function that is given by

$$f(x) = 5x + 2 + E_{-1}(x)$$

where  $E_{-1}$  is  $o(x + 1)$ . Determine  $f'(-1)$  and determine an equation for the line  $L$  that is tangent to  $f$  at  $(-1, f(-1))$ .

2. Take  $f(x) = x^3$ . Write the local linear approximation of  $f$  at  $a = 1$ . Use your local linear approximation to approximate  $(1.05)^3$ .

3. The following functions are continuous at  $x_0 = 1$ , but are not differentiable at  $x_0 = 1$ . Explain why.

a)  $f(x) = |x - 1|$

b)  $f(x) = \sqrt{x - 1}$

4. Calculate the derivative of each function by decomposing it into a sum and or product of simpler functions and by using the appropriate derivative rule.

a)  $f(x) = 5x^4 + \sin(x) - e$

b)  $f(x) = x^{4/5} \exp_5(x) + \sqrt{x} \tan(x)$

5. Calculate the derivative of each function  $f$ .

a)  $f(x) = \frac{1}{\sin(x)}$

b)  $f(x) = \frac{x+3}{\ln(x)}$

c)  $f(x) = \exp(x) \cdot \frac{2x}{\exp(x) + \cos(x)}$

6. Calculate the derivative of each function  $f$ .

a)  $f(x) = \sqrt{4\cos(x) + \ln(x)}$

b)  $f(x) = \sin(e^x) \cos(3x + 1)$

7. For the function  $f$  given below, decompose  $f$  into simpler functions in order to find a formula for  $f'(x)$ :

$$f(x) = (3x + 5)^4 \sqrt{x^5 - x} + g(3x + 1) + (g(x))^3,$$

where  $g$  is a differentiable function. Your answer will involve  $g'$  and  $g$ .

8. Use Newton’s Method to approximate the value  $5^{\frac{1}{5}}$ . Start with an initial guess of  $x_1 = 1$  and apply the method three times.